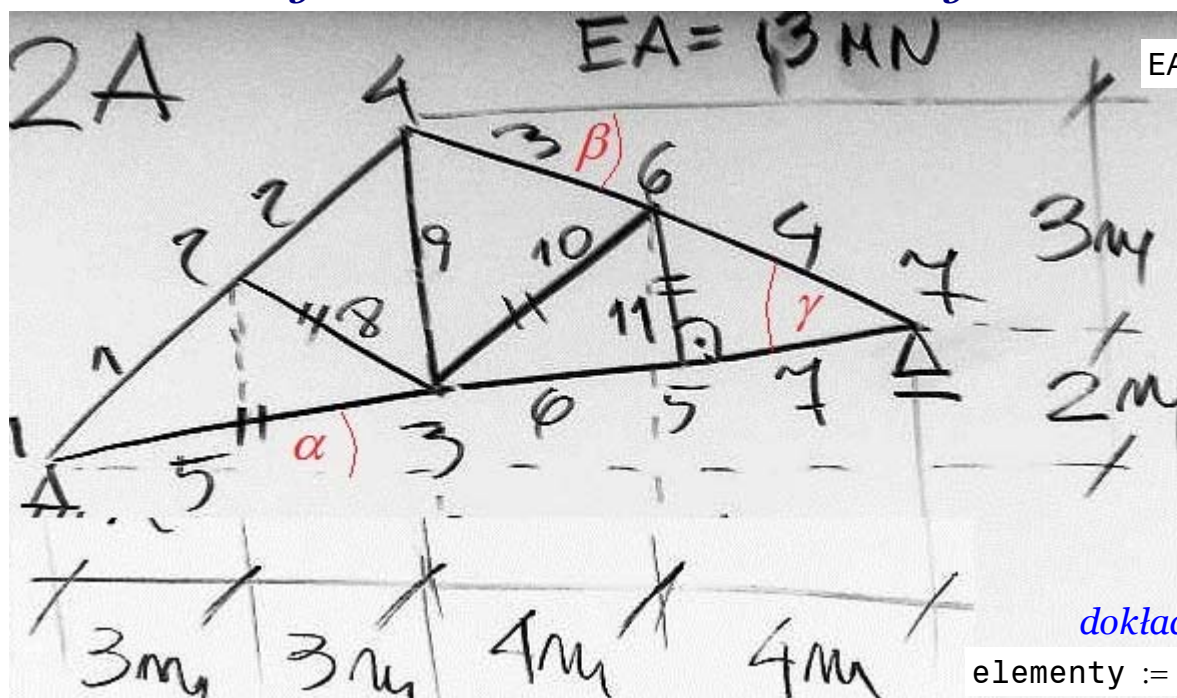


Macierze sztywności elementów kratownicy 2A



EA := 13MN

dokładność $\pm 0.5 \text{ kN/m}$

elementy := (5, 8, 10, 11)

$$\alpha := \operatorname{atan}\left(\frac{2}{14}\right) = 8.13010 \cdot \text{deg} \quad \beta := \operatorname{atan}\left(\frac{3}{8}\right) = 20.5560 \cdot \text{deg}$$

$$\gamma := \beta + \alpha = 28.686148 \cdot \text{deg}$$

$$Y3 := 2\text{m} \cdot \frac{6}{14} = 0.85714 \text{ m}$$

$$Y6 := 2\text{m} + 3\text{m} \cdot \frac{4}{8} = 3.5 \text{ m}$$

$$L4 := \sqrt{(4\text{m})^2 + (Y6 - 2\text{m})^2} = 4.272 \text{ m}$$

$$L11 := L4 \cdot \sin(\gamma) = 2.05061 \text{ m}$$

$$K = \begin{bmatrix} \mathbf{J^1 + J^5} & -\mathbf{J^1} & -\mathbf{J^5} & & & & \\ & \mathbf{J^1 + J^2 + J^8} & -\mathbf{J^8} & -\mathbf{J^2} & & & \\ & & \mathbf{J^5 + J^6 + J^8} & -\mathbf{J^9} & -\mathbf{J^6} & -\mathbf{J^{10}} & \\ & & +\mathbf{J^9 + J^{10}} & & & & \\ & & & \mathbf{J^2 + J^3 + J^9} & & -\mathbf{J^3} & \\ \text{Symetria} & \text{Symetria} & \text{Symetria} & \text{Symetria} & \mathbf{J^6 + J^7 + J^{11}} & -\mathbf{J^{11}} & -\mathbf{J^7} \\ & & & & & \mathbf{J^3 + J^4 + J^{10} + J^{11}} & -\mathbf{J^4} \\ & & & & & & \mathbf{J^4 + J^7} \end{bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{matrix}$$

Element "5" - blok macierzy sztywności

$$L_x := 6\text{m}$$

$$L_y := Y_3 = 0.857143\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 6.060915\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 2102 & 300 \\ 300 & 43 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$

Element "8" - blok macierzy sztywności

$$L_x := 3\text{m} = 3\text{m}$$

$$L_y := Y_3 - \frac{5\text{m}}{2} = -1.642857\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 3.420377\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 2924 & -1601 \\ -1601 & 877 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$

Element "10" - blok macierzy sztywności

$$L_x := 4\text{m} = 4\text{m}$$

$$L_y := Y_6 - Y_3 = 2.642857\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 4.794235\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 1888 & 1247 \\ 1247 & 824 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$

Element "11" - blok macierzy sztywności

$$L_x := L_{11} \cdot \sin(\alpha) = 0.29\text{m}$$

$$L_y := -L_{11} \cdot \cos(\alpha) = -2.030000\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 2.05061\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 127 & -888 \\ -888 & 6213 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$