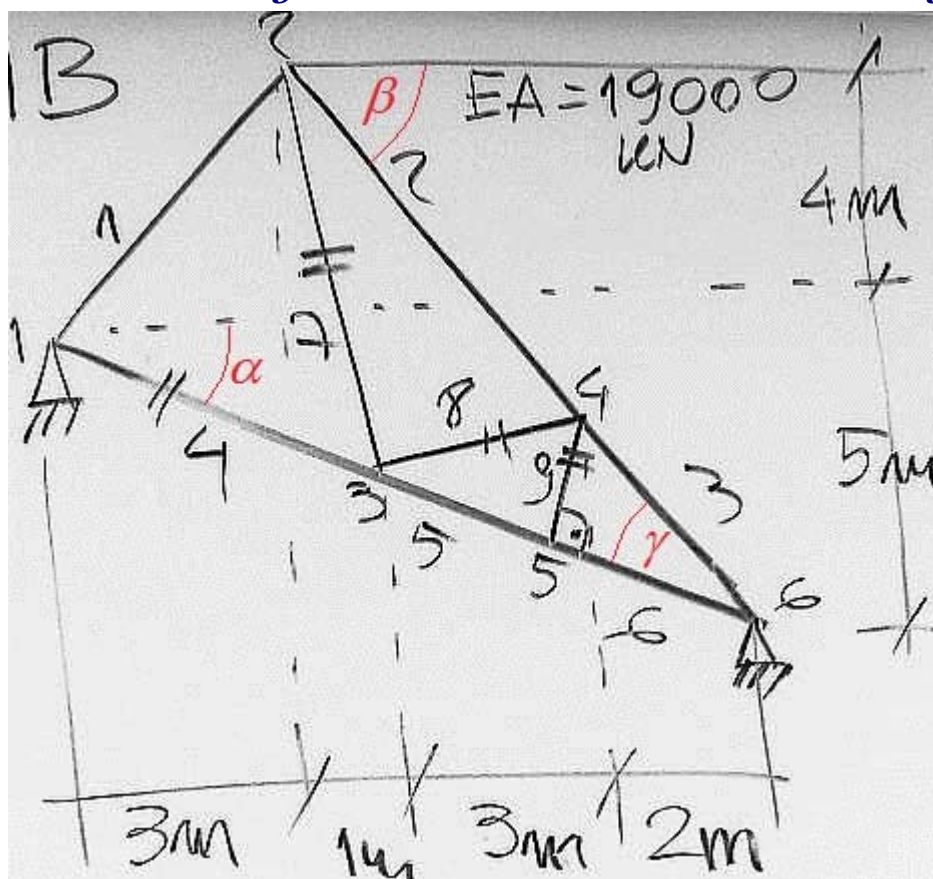


## Macierze sztywności elementów kratownicy 1B



$$\alpha := \operatorname{atan}\left(\frac{5}{9}\right)$$

$$\beta := \operatorname{atan}\left(\frac{9}{6}\right)$$

$$\gamma := \beta - \alpha = 0.4757$$

$$\gamma = 27.255 \cdot \text{deg}$$

$$EA := 19\text{MN}$$

dokładność  $\pm 0.5\text{kN/m}$

$$\text{elementy} := (4, 7, 8, 9)$$

$$Y3 := -5\text{m} \cdot \frac{4}{9} = -2.22222\text{ m} \quad Y4 := 9\text{m} \cdot \frac{2}{6} - 5\text{m} = -2\text{ m}$$

$$Y5 := 3\text{m} \cdot \frac{8}{13} = 1.84615\text{ m}$$

$$L3 := \sqrt{(2\text{m})^2 + (3\text{m})^2} = 3.60555\text{ m}$$

$$L9 := L3 \cdot \sin(\gamma) = 1.65119\text{ m}$$

$$K = \begin{bmatrix} \mathbf{J^1 + J^4} & \mathbf{-J^1} & \mathbf{-J^4} & & & \\ & \mathbf{J^1 + J^2 + J^7} & \mathbf{-J^7} & \mathbf{-J^2} & & \\ & & \mathbf{J^4 + J^5 + J^7 + J^8} & \mathbf{-J^8} & \mathbf{-J^5} & \\ & & & \mathbf{J^2 + J^3 + J^7 + J^9} & \mathbf{-J^9} & \mathbf{-J^3} \\ \text{Symetria} & \text{Symetria} & \text{Symetria} & \text{Symetria} & \mathbf{J^5 + J^6 + J^9} & \mathbf{-J^6} \\ & & & & & \mathbf{J^3 + J^6} \end{bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

### Element "4" - blok macierzy sztywności

$$L_x := 4\text{m} = 4\text{m}$$

$$L_y := Y_3 = -2.222222\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 4.575836\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 3173 & -1763 \\ -1763 & 979 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$

### Element "7" - blok macierzy sztywności

$$L_x := 1\text{m} = 1\text{m}$$

$$L_y := Y_3 - 4\text{m} = -6.222222\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 6.302067\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 76 & -472 \\ -472 & 2939 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$

### Element "8" - blok macierzy sztywności

$$L_x := 3\text{m}$$

$$L_y := Y_4 - Y_3 = 0.222222\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 3.008219\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 6282 & 465 \\ 465 & 34 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$

### Element "9" - blok macierzy sztywności

$$L_x := L_9 \cdot \sin(\alpha) = 0.802\text{m}$$

$$L_y := L_9 \cdot \cos(\alpha) = 1.443396\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 1.651186\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix}$$

$$J = \begin{pmatrix} 2714 & 4885 \\ 4885 & 8793 \end{pmatrix} \cdot \frac{\text{kN}}{\text{m}}$$