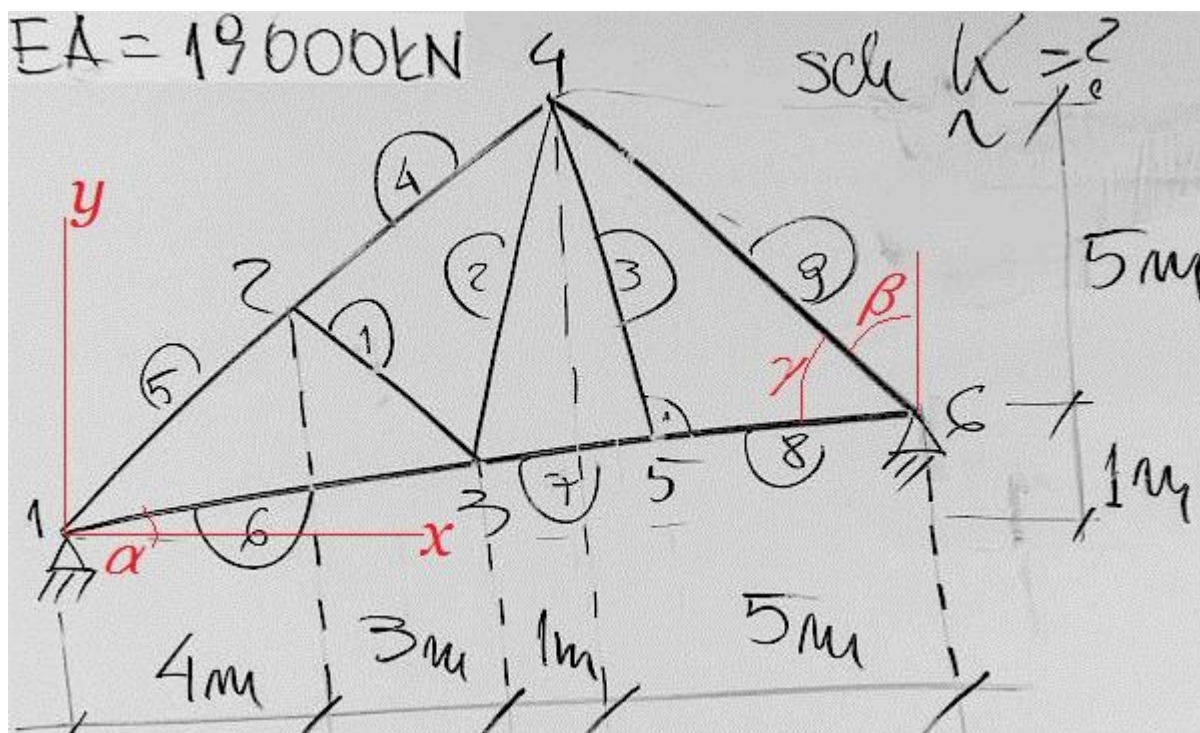


## K1 - Macierze sztywności elementów kratownicy



elementy := (1, 2, 3, 4)

EA := 19MN

dokładność  $\pm 0.5 \text{ kN/m}$

$$\alpha := \operatorname{atan}\left(\frac{1}{13}\right) = 4.399 \cdot \text{deg}$$

$$\beta := \operatorname{atan}\left(\frac{5}{5}\right) = 45 \cdot \text{deg}$$

$$\gamma := \frac{\pi}{2} - \beta + \alpha = 49.39871 \cdot \text{deg}$$

$$L9 := 5\text{m} \cdot \sqrt{2} = 7.07107\text{m}$$

$$L3 := L9 \cdot \sin(\gamma) = 5.36875\text{m}$$

$$Y2 := 6\text{m} \cdot \frac{4}{8} = 3\text{m}$$

$$Y3 := 1\text{m} \cdot \frac{7}{13} = 0.53846\text{m}$$

$$X5 := 8\text{m} + L3 \cdot \sin(\alpha) = 8.41176\text{m}$$

$$Y5 := 1\text{m} \cdot \frac{X5}{13\text{m}} = 0.64706\text{m}$$

$$K = \begin{bmatrix} \mathbf{J^5 + J^6} & -\mathbf{J^5} & -\mathbf{J^6} & & & \\ & \mathbf{J^1 + J^4 + J^5} & -\mathbf{J^1} & -\mathbf{J^4} & & \\ & & \mathbf{J^1 + J^2 + J^6 + J^7} & -\mathbf{J^2} & -\mathbf{J^7} & \\ & & & \mathbf{J^2 + J^3 + J^4 + J^9} & -\mathbf{J^3} & -\mathbf{J^9} \\ \text{Symetria} & \text{Symetria} & \text{Symetria} & \text{Symetria} & \mathbf{J^3 + J^7 + J^8} & -\mathbf{J^8} \\ & & & & & \mathbf{J^8 + J^9} \end{bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix}$$

### *Element "1" - blok macierzy sztywności*

$$L_x := 3\text{m} = 3.00000\text{m}$$

$$L_y := Y_3 - Y_2 = -2.46154\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 3.880615\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix} \quad J = \begin{bmatrix} 2926 & -2401 \\ (-2401) & 1970 \end{bmatrix} \frac{\text{kN}}{\text{m}}$$

### *Element "2" - blok macierzy sztywności*

$$L_x := 1\text{m} = 1\text{m}$$

$$L_y := 6\text{m} - Y_3 = 5.461538\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 5.552333\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix} \quad J = \begin{bmatrix} 111 & 606 \\ (606) & 3311 \end{bmatrix} \frac{\text{kN}}{\text{m}}$$

### *Element "3" - blok macierzy sztywności*

$$L_x := X_5 - 8\text{m} = 0.411765\text{m}$$

$$L_y := Y_5 - 6\text{m} = -5.352941\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 5.368755\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix} \quad J = \begin{bmatrix} 21 & -271 \\ (-271) & 3518 \end{bmatrix} \frac{\text{kN}}{\text{m}}$$

### *Element "4" - blok macierzy sztywności*

$$L_x := 4\text{m} = 4\text{m}$$

$$L_y := 6\text{m} - Y_2 = 3.000000\text{m}$$

$$L := \sqrt{(L_x)^2 + (L_y)^2} = 5\text{m}$$

$$J := \frac{EA}{(L)^3} \cdot \begin{bmatrix} (L_x)^2 & L_x \cdot L_y \\ L_x \cdot L_y & (L_y)^2 \end{bmatrix} \quad J = \begin{bmatrix} 2432 & 1824 \\ (1824) & 1368 \end{bmatrix} \frac{\text{kN}}{\text{m}}$$