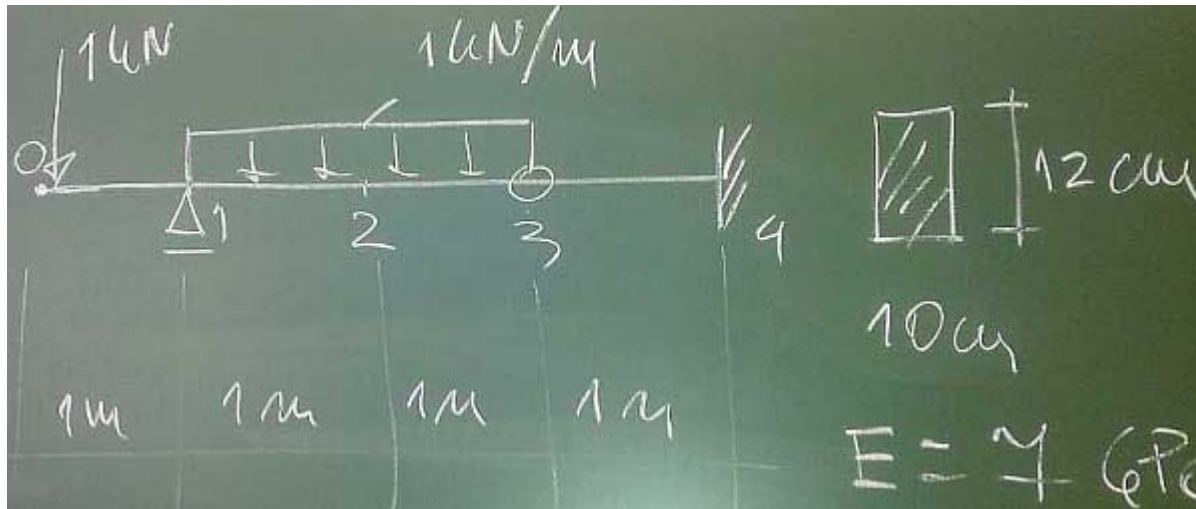


Metoda różnic skończonych - ugięcie belki



$$R1 := \frac{P \cdot 3m + q \cdot 2m \cdot 1m}{2m}$$

$$M1(x) := -P \cdot x \quad M2(x) := M1(x) - q \cdot \frac{(x - 1m)^2}{2} + R1 \cdot (x - 1m)$$

$$M3(x) := M2(x) + q \cdot \frac{(x - 3m)^2}{2}$$

$$P := 1kN \quad q := 1 \frac{kN}{m} \quad E := 7GPa$$

$$b := 10cm \quad h := 12cm$$

$$L := 4m \quad J := b \cdot \frac{h^3}{12} = 1440 \cdot cm^4$$

$$n := 4 \quad \Delta := \frac{L}{n} = 1m$$

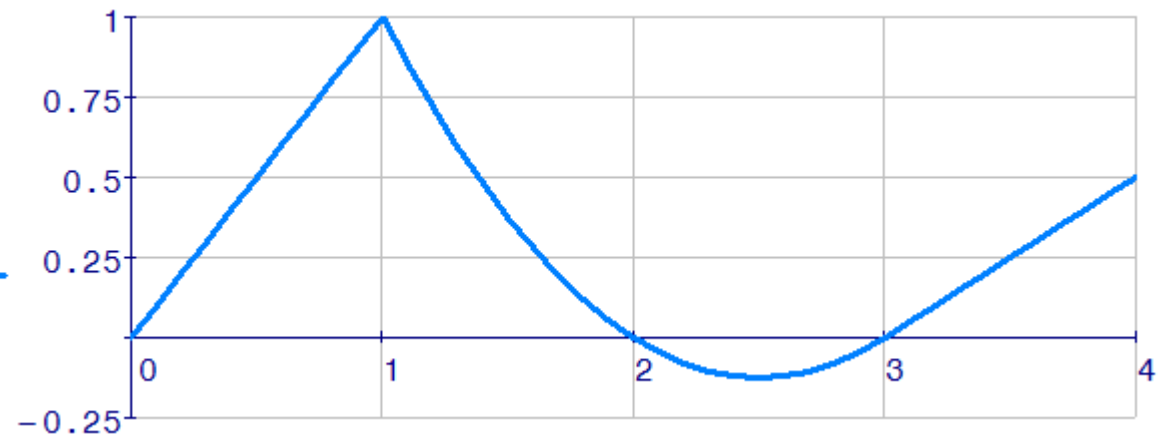
$$\alpha := \frac{\Delta^2}{E \cdot J} = 9.92063 \cdot \frac{1}{MN}$$

dokładność $y \pm 0.005mm$

$$M = \begin{array}{|c|c|} \hline & 0 \\ \hline 0 & 0 \\ \hline 1 & -1 \\ \hline 2 & 0 \\ \hline 3 & 0 \\ \hline 4 & -0.5 \\ \hline \end{array} \cdot \text{kN} \cdot \text{m}$$

$$X = \begin{array}{|c|c|} \hline & 0 \\ \hline 0 & 0 \\ \hline 1 & 1 \\ \hline 2 & 2 \\ \hline 3 & 3 \\ \hline 4 & 4 \\ \hline \end{array} \text{m}$$

$$\frac{-M}{\text{kN} \cdot \text{m}}$$



Warunki brzegowe

$$y_1 = 0 \quad y_4 = 0 \quad \varphi_4 = 0 \quad \text{-----} > \quad 2 y_3 = \alpha M_4$$

$$\alpha = 9.92063 \cdot \frac{1}{\text{MN}}$$

Równania MRS

$$y_0 - 2 y_1 + y_2 = \alpha M_1$$

$$y_1 - 2 y_2 + y_3 = \alpha M_2$$

$$2 y_3 = \alpha M_4$$

$$y = \begin{array}{|c|c|} \hline & 0 \\ \hline 0 & -8.68 \\ \hline 1 & 0.00 \\ \hline 2 & -1.24 \\ \hline 3 & -2.48 \\ \hline 4 & 0.00 \\ \hline \end{array} \cdot \text{mm}$$