

Grupa B2

Zad 1

$$\underline{\underline{L}} := 5\text{m} \quad P_0 := 12\text{kN} \quad b := 11\text{cm} \quad h := 8\text{cm} \quad \underline{\underline{g}} := 1\text{cm} \quad h_1 := h - 2g \quad b_1 := b - 2g$$

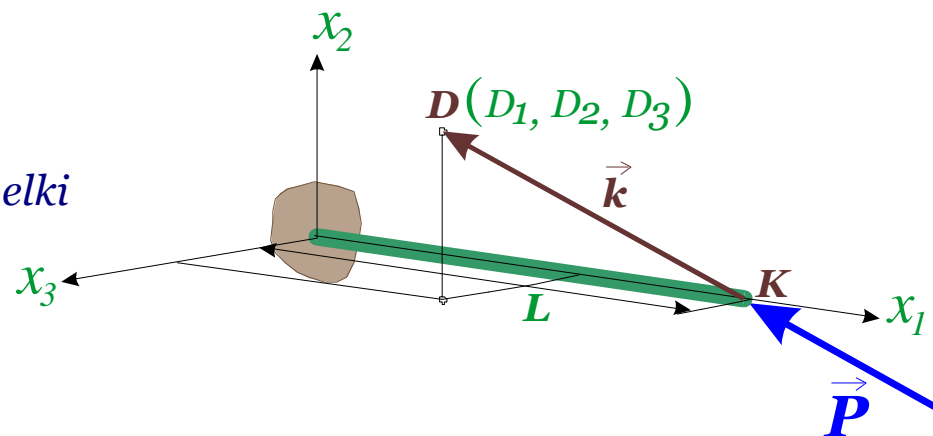
$$D := \begin{pmatrix} -3 \\ -4 \\ 5 \end{pmatrix} \text{m} \quad - \text{współrzędne punktu przez który przechodzi kierunek siły}$$

$$\underline{\underline{K}} := \begin{pmatrix} L \\ 0 \\ 0 \end{pmatrix} \quad - \text{współrzędne punktu } K, \text{ obciążonego końca belki}$$

$$k := D - K \quad - \text{wektor kierunkowy siły} \quad k = \begin{pmatrix} -8 \\ -4 \\ 5 \end{pmatrix} \text{m}$$

$$Lk := \sqrt{(k_1)^2 + (k_2)^2 + (k_3)^2} = 10.24695 \text{m} \quad - \text{moduł (długość) wektora kierunkowego}$$

$$\underline{\underline{c}} := \frac{1}{Lk} \cdot k = \begin{pmatrix} -0.78072 \\ -0.39036 \\ 0.48795 \end{pmatrix} \quad - \text{kosinusy kierunkowe wektora siły } P$$



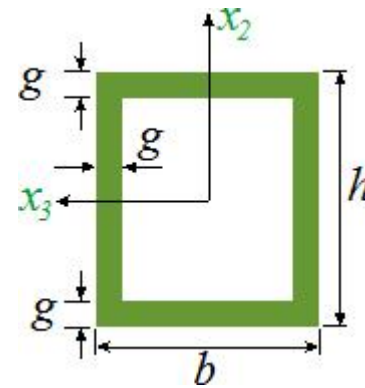
$$P := P_0 \cdot c \quad - \text{składowe wektora siły} \quad P = \begin{pmatrix} -9.369 \\ -4.684 \\ 5.855 \end{pmatrix} \cdot \text{kN}$$

$$N := P_1 \quad T_2 := P_2 \quad T_3 := P_3$$

$$N = -9.36864 \cdot \text{kN} \quad T_2 = -4.68432 \cdot \text{kN} \quad T_3 = 5.8554 \cdot \text{kN}$$

$$M_2 := -T_3 \cdot L \quad M_3 := T_2 \cdot L$$

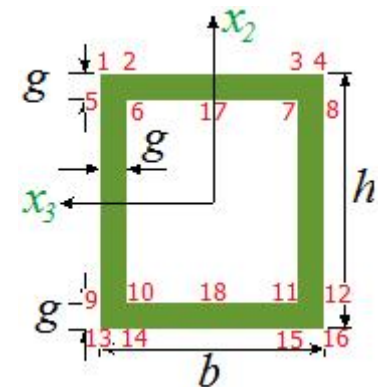
$$M_2 = -29.27700 \cdot \text{kN} \cdot \text{m} \quad M_3 = -23.42160 \cdot \text{kN} \cdot \text{m}$$



$$A := h \cdot b - h_1 \cdot b_1 = 34 \cdot \text{cm}^2$$

$$J_3 := \frac{b \cdot h^3}{12} - \frac{b_1 \cdot h_1^3}{12} = 3.07333 \times 10^2 \cdot \text{cm}^4$$

$$J_2 := \frac{h \cdot b^3}{12} - \frac{h_1 \cdot b_1^3}{12} = 5.22833 \times 10^2 \cdot \text{cm}^4$$



Naprężenia w punkcie A

$$y := x2_{id} \quad z := x3_{id} \quad a2 := b2_{id} \quad a3 := b3_{id}$$

$$S3 := St3_{id} \quad S2 := St2_{id}$$

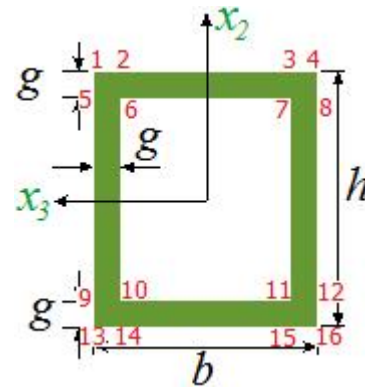
$$\sigma_{11} := \frac{N}{A} - \frac{M3 \cdot y}{J3} + \frac{M2 \cdot z}{J2} = 610.063 \cdot \text{MPa}$$

$$\tau_{12} := \frac{T2 \cdot S3}{a3 \cdot J3} = 0.000 \cdot \text{MPa}$$

$$\tau_{13} := \frac{T3 \cdot S2}{a2 \cdot J2} = 0.000 \cdot \text{MPa}$$

$$\sigma_{\text{HMH}} := \sqrt{\sigma_{11}^2 + 3 \cdot (\tau_{12}^2 + \tau_{13}^2)} = 610.063 \cdot \text{MPa}$$

id := 4



$$y = 4 \cdot \text{cm}$$

$$z = -5.5 \cdot \text{cm}$$

$$a2 = 8 \cdot \text{cm}$$

$$a3 = 11 \cdot \text{cm}$$

$$S2 = 0 \cdot \text{cm}^3$$

$$S3 = 0 \cdot \text{cm}^3$$

Naprężenia w punkcie B

$$\underline{y} := x2_{id} \quad \underline{z} := x3_{id} \quad \underline{a2} := b2_{id} \quad \underline{a3} := b3_{id}$$

$$\underline{S3} := St3_{id} \quad \underline{S2} := St2_{id}$$

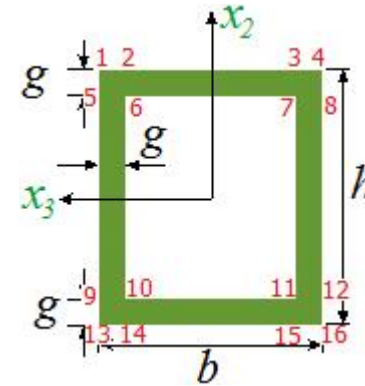
$$\underline{\sigma_{11}} := \frac{N}{A} - \frac{M3 \cdot y}{J3} + \frac{M2 \cdot z}{J2} = 20.603 \cdot \text{MPa}$$

$$\underline{\tau_{12}} := \frac{T2 \cdot S3}{a3 \cdot J3} = -2.934 \cdot \text{MPa}$$

$$\underline{\tau_{13}} := \frac{T3 \cdot S2}{a2 \cdot J2} = 2.240 \cdot \text{MPa}$$

$$\underline{\sigma_{HHH}} := \sqrt{\sigma_{11}^2 + 3 \cdot (\tau_{12}^2 + \tau_{13}^2)} = 21.572 \cdot \text{MPa}$$

$$\underline{id} := 11$$



$$y = -3 \cdot \text{cm}$$

$$z = -4.5 \cdot \text{cm}$$

$$a2 = 2 \cdot \text{cm}$$

$$a3 = 2 \cdot \text{cm}$$

$$S2 = 40 \cdot \text{cm}^3$$

$$S3 = 38.5 \cdot \text{cm}^3$$

Naprężenia w punkcie C

id := 17

$$\underline{y} := x2_{id} \quad \underline{z} := x3_{id} \quad \underline{a2} := b2_{id} \quad \underline{a3} := b3_{id}$$

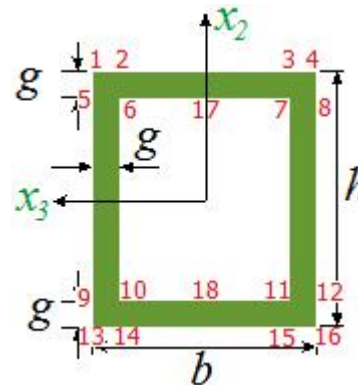
$$\underline{S3} := St3_{id} \quad \underline{S2} := St2_{id}$$

$$\underline{\sigma_{11}} := \frac{N}{A} - \frac{M3 \cdot y}{J3} + \frac{M2 \cdot z}{J2} = 225.872 \cdot \text{MPa}$$

$$\underline{\tau_{12}} := \frac{T2 \cdot S3}{a3 \cdot J3} = -0.658 \cdot \text{MPa}$$

$$\underline{\tau_{13}} := \frac{T3 \cdot S2}{a2 \cdot J2} = 3.374 \cdot \text{MPa}$$

$$\underline{\sigma_{HHH}} := \sqrt{\sigma_{11}^2 + 3 \cdot (\tau_{12}^2 + \tau_{13}^2)} = 225.95 \cdot \text{MPa}$$



$$y = 3 \cdot \text{cm}$$

$$z = 0 \cdot \text{cm}$$

$$a2 = 2 \cdot \text{cm}$$

$$a3 = 11 \cdot \text{cm}$$

$$S2 = 60.25 \cdot \text{cm}^3$$

$$S3 = 47.5 \cdot \text{cm}^3$$